

Wetting of hairy surfaces

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Wetting and Geometry

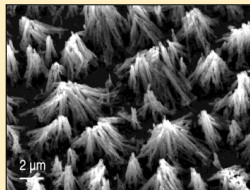
Geometry \rightarrow Wetting

- Capillary condensation.
- Wedge wetting.
- Superhydrophobic surfaces.¹



Geometry \leftarrow Wetting

- Deformation of elastic surfaces.
- Collapse of patterned substrates.¹

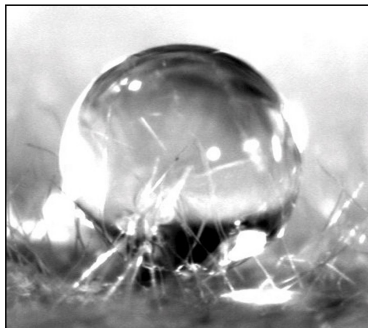


Goal: Geometry \Leftrightarrow Wetting.

¹Lau et al, Nanoletters **3** (2003), 1701

An Intriguing Example: The Lady's Mantle

- Leaves covered with hydrophilic hairs.¹
- Droplets can be suspended in the fur.



- Behaviour attributed to elasticity of the hairs.

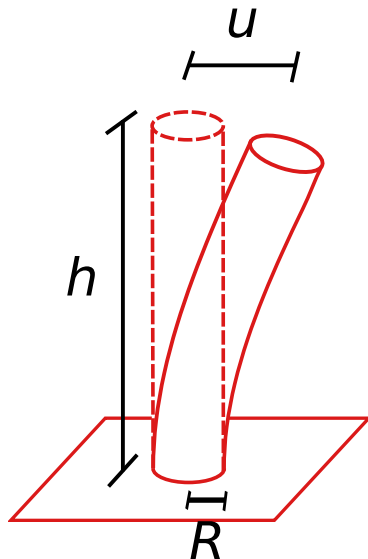
¹Otten & Herminghaus, Langmuir **20** (2004) 2405

Simple Model I: Elastic Energy

- Elastic Energy

$$E_{\text{el}} = \frac{3\pi ER^4}{8h^3} u^2$$

- $E \equiv$ Young's modulus.
- $R \equiv$ radius of posts.
- $h \equiv$ height.
- $u \equiv$ deviation from equilibrium position.

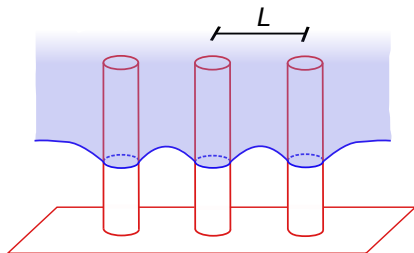


Simple Model II: Capillary Interaction

- Capillary Energy

$$E_{\text{cap}} = 2\pi\sigma R^2 \ln(qL) \cos^2 \theta$$

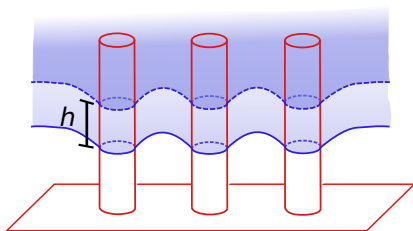
- $\sigma \equiv$ surface tension.
- $\theta \equiv$ contact angle.
- $q^{-1} \equiv$ capillary length.
- $L \equiv$ distance between centres of posts.



Simple Model III: Wetting Energy

- Wetting Energy

$$E_{\text{wet}} = 2\pi Rh\sigma \cos\theta$$



Some Remarks

- Thermal fluctuations are too small.
- Non-dimensionalising we have

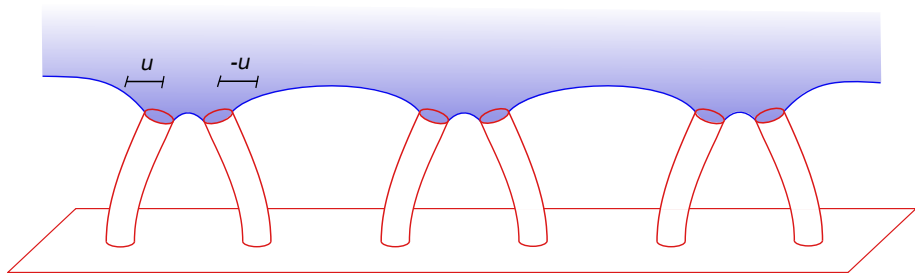
$$\bar{H} = \bar{h} \cos \theta + \frac{\bar{k}}{\bar{h}^3} \bar{u} + \ln(\bar{L}) \cos^2 \theta$$

- Essential parameter:

$$\bar{k} = \frac{3ER}{8\sigma}$$

- The Young's Modulus of the Lady's Mantle hairs is not known but a lower estimate is $\bar{k} \gtrsim 50$.

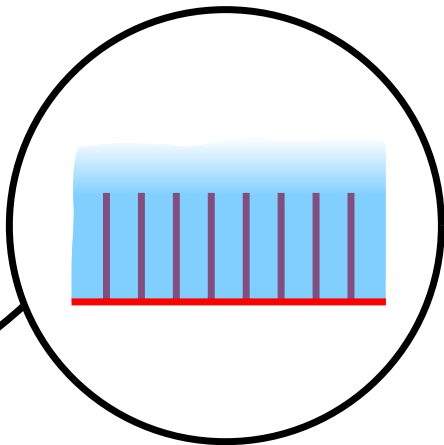
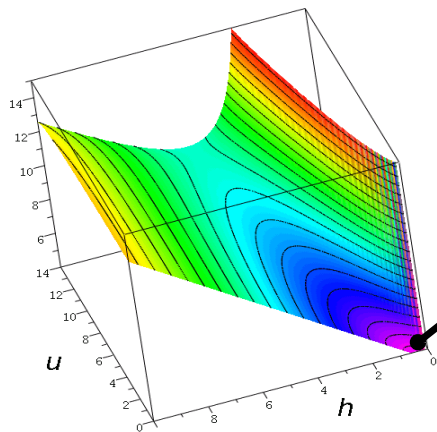
1D Toy Model I



$$H(u, h) = h \cos \theta + \frac{k}{h^3} u^2 + \frac{\ln(L - 2u) \cos^2 \theta}{2} + \frac{\ln(L + 2u) \cos^2 \theta}{2}$$

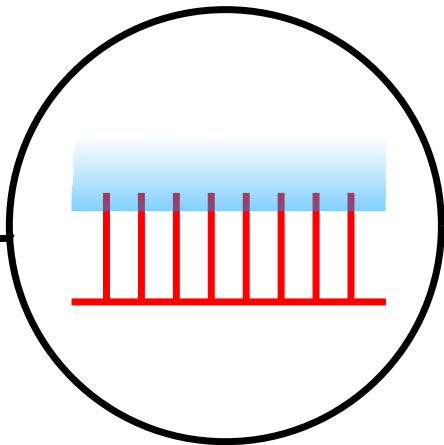
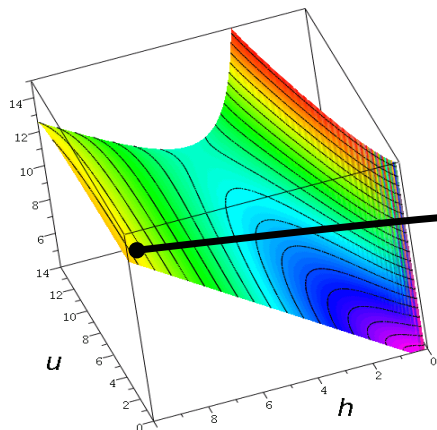
$$u \in \left[0, \frac{L - 2}{2} \right]$$

1D Toy Model II



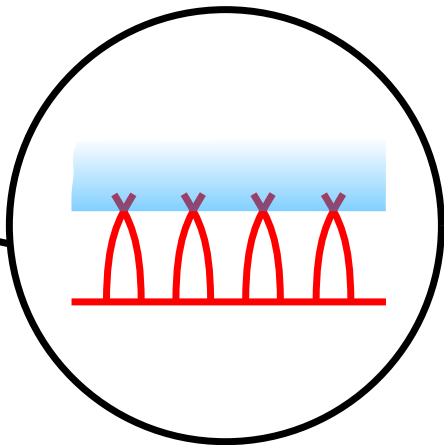
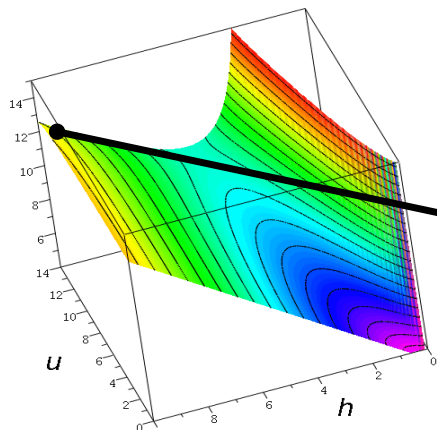
$$k = 1, L = 30, \cos \theta = 1.$$

1D Toy Model II



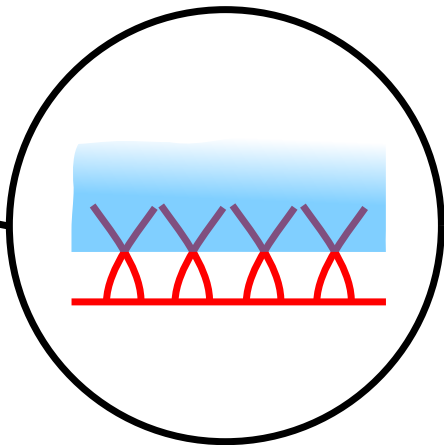
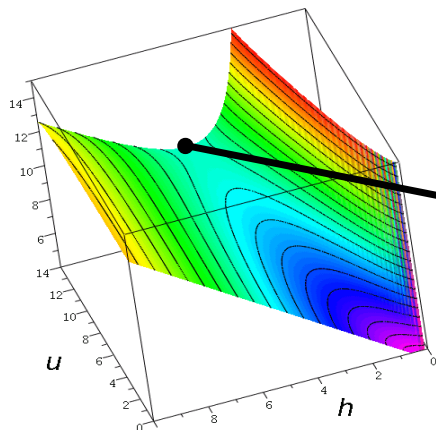
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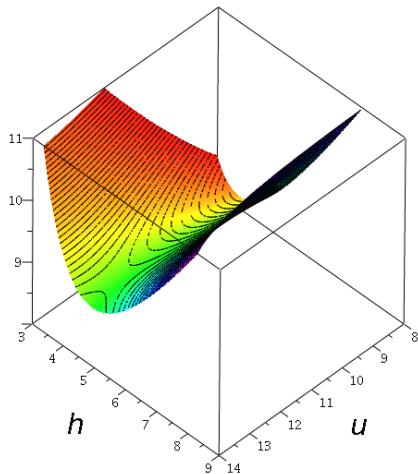
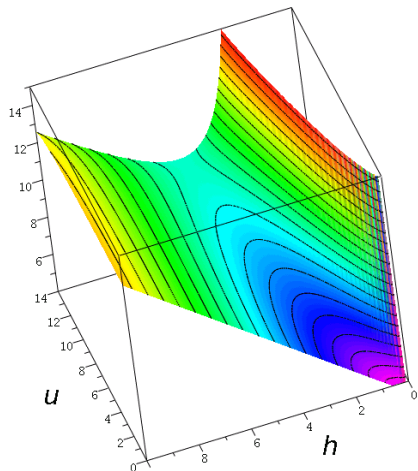
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Simple Estimates

- Posts bend if

$$h^3 > \frac{kL^2}{2 \cos^2 \theta}$$

- Elastic energy balances wetting energy when

$$h^{*4} = \frac{k(L-2)^2(n^2-1)}{4 \cos \theta}$$

- Cluster holds together if

$$(L-2)^2 > 2^{10} k \frac{(n-1)^4}{(n^2-1)^3 (\cos \theta)^5}$$

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Simple Estimates II

- $(k = 1, \cos \theta = 1) \Rightarrow$

$$L \gtrsim 8, h^* \simeq 5.$$

- Lady's Mantle: $(k = 50, \cos \theta = 1/2) \Rightarrow$

$$L \gtrsim 250, h^* \simeq 50!$$

- With bigger clusters and pair interactions L can be smaller.
- 1D \neq 2D: For Lady's Mantle

$$L \gtrsim 90, h^* \simeq 30.$$

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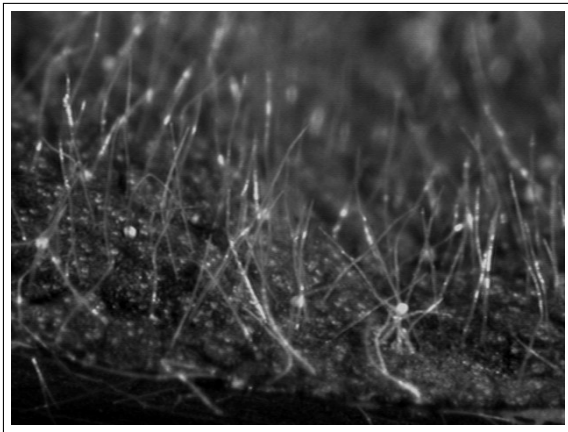
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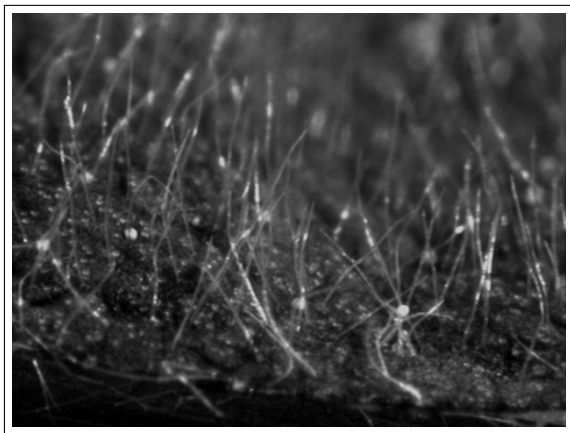
Back to the Lady's Mantle

Thanks to Valentin Blickle (and mom)



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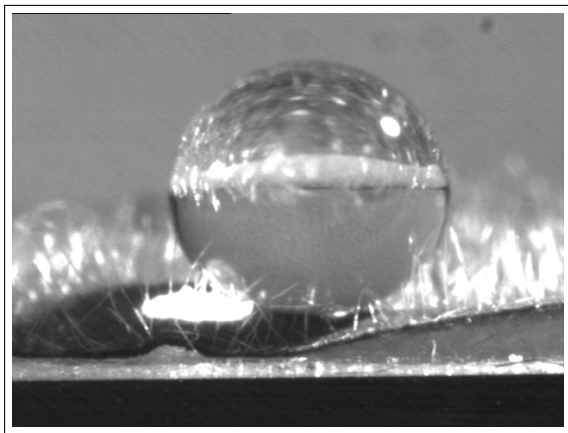
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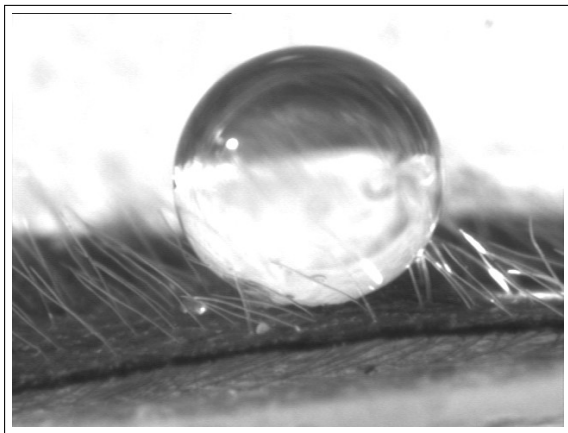
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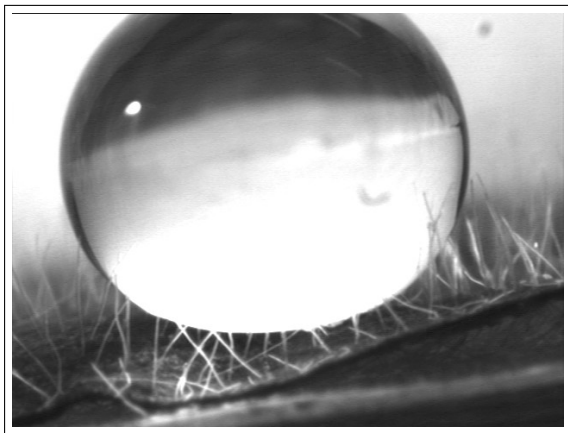
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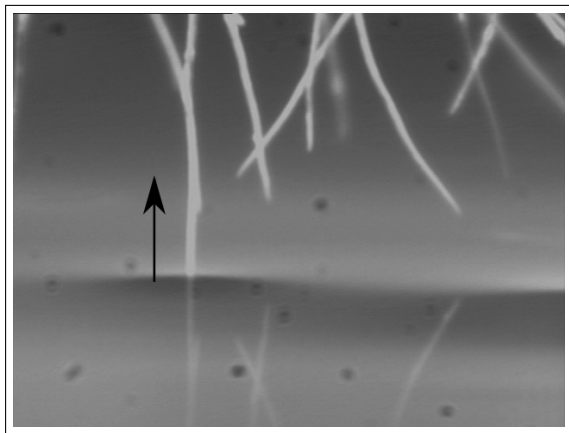
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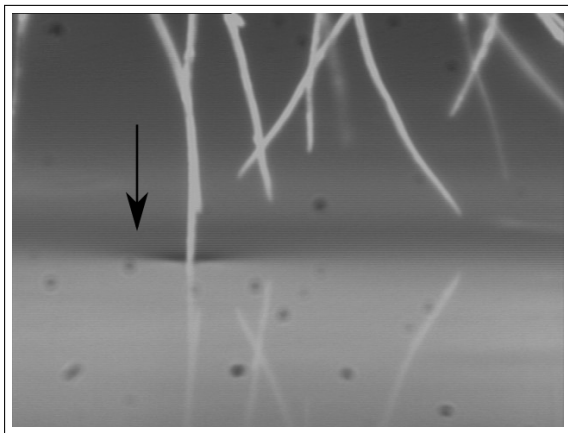
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- Accurate estimate of energy of collapsed posts.
- Many body capillary interactions.
- Influence of lattice/disorder.
- Influence of inclined posts.
- Curvature of interface.
- Experimental verification of contact angle and hairs' Young's modulus.